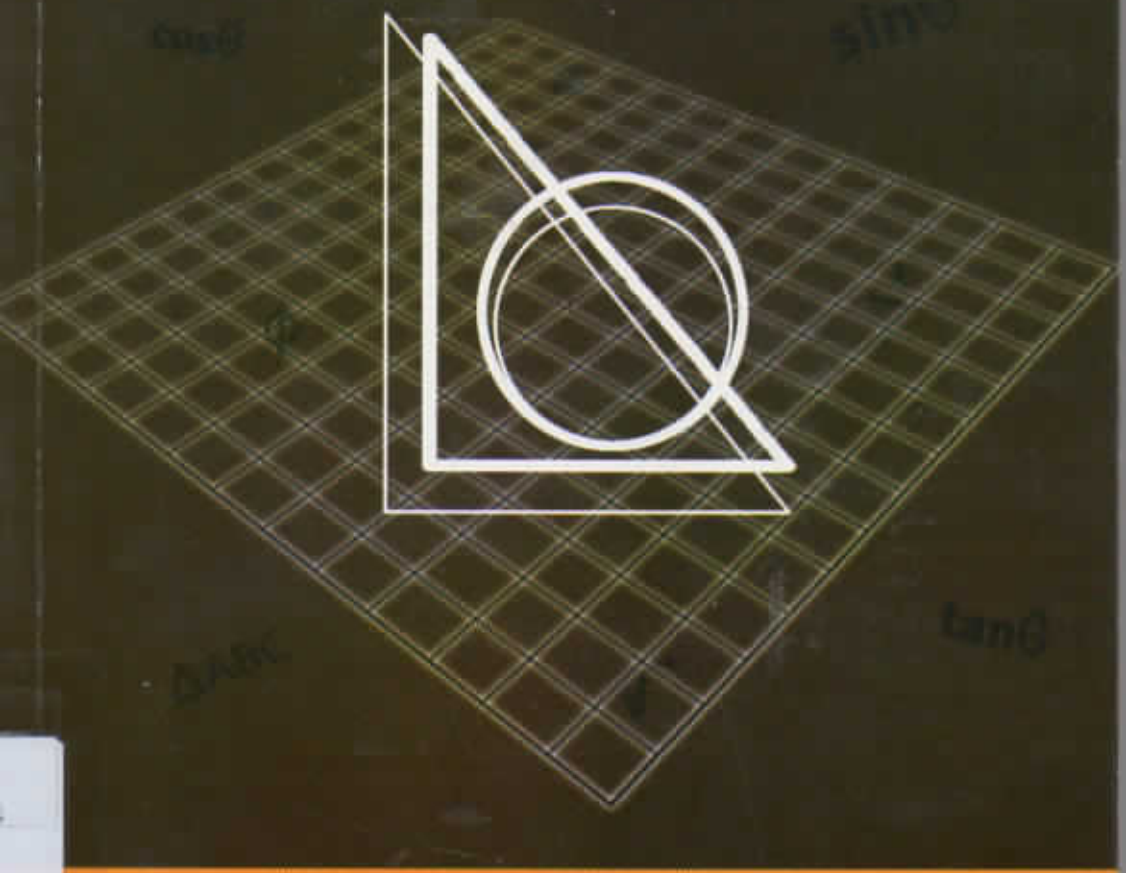
PLANE AND SPHERICAL TRIGONOMETRY

A TETRAHEDRON APPROACH



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PLANE & SPHERICAL TRIGONOMETRY

A Tetrahedron Approach

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